

# Formulario per il corso di Statistica CLEAM, AA 20/21

Media aritmetica	Varianza	Percentile
$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$	$\hat{\sigma}^2 = \frac{1}{n} \sum_{i=1}^n x_i^2 - \bar{x}^2$	$x_p = x_{\inf;j_p} + \frac{p - F_{j_p-1}}{f_{j_p}} \cdot (x_{\sup;j_p} - x_{\inf;j_p})$
Binomiale		Poisson
$f(x) = \binom{n}{x} \pi^x (1-\pi)^{n-x}$		$f(x) = \frac{\lambda^x}{x!} e^{-\lambda}$
Test $Z$ , 1 Campione	Test $t$ , 1 Campione	Proporzione, 1 Campione
$z_{\text{obs}} = \frac{\hat{\mu} - \mu_0}{\sigma/\sqrt{n}}$	$t_{\text{obs}} = \frac{\hat{\mu} - \mu_0}{S/\sqrt{n}}$ $S^2 = \frac{n}{n-1} \hat{\sigma}^2$	$z_{\text{obs}} = \frac{\hat{\pi} - \pi_0}{\sqrt{\frac{\pi_0(1-\pi_0)}{n}}}$
Test $t$ , 2 Campioni Omogeneità	Test $t$ , 2 Campioni Eterogeneità	Proporzione, 2 Campioni
$t_{\text{obs}} = \frac{\hat{\mu}_A - \hat{\mu}_B}{\sqrt{\frac{S_p^2}{n_A} + \frac{S_p^2}{n_B}}}$ $S_p^2 = \frac{n_A \hat{\sigma}_A^2 + n_B \hat{\sigma}_B^2}{n_A + n_B - 2}$	$t_{\text{obs}} = \frac{\hat{\mu}_A - \hat{\mu}_B}{\sqrt{\frac{S_A^2}{n_A} + \frac{S_B^2}{n_B}}}$	$z_{\text{obs}} = \frac{\hat{\pi}_A - \hat{\pi}_B}{\sqrt{\frac{\hat{\pi}_C(1-\hat{\pi}_C)}{n_A} + \frac{\hat{\pi}_C(1-\hat{\pi}_C)}{n_B}}}$ $\hat{\pi}_C = \frac{\#\{\text{successi A}\} + \#\{\text{successi B}\}}{n_A + n_B}$ $= \frac{n_A \hat{\pi}_A + n_B \hat{\pi}_B}{n_A + n_B}$
Regressione		
$\text{cov}(x, y) = \frac{1}{n} \sum_{i=1}^n x_i y_i - \bar{x} \bar{y}$ $r = \frac{\text{cov}(x, y)}{\hat{\sigma}_X \hat{\sigma}_Y}$	$\hat{\beta}_1 = \frac{\text{cov}(x, y)}{\hat{\sigma}_X^2}$ $\hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x}$	$\hat{\sigma}_\varepsilon^2 = \hat{\sigma}_Y^2 (1 - r^2)$ $S_\varepsilon^2 = \frac{n}{n-2} \hat{\sigma}_\varepsilon^2$
$V(\hat{\beta}_1) = \frac{\sigma_\varepsilon^2}{n \hat{\sigma}_X^2}$	$V(\hat{\beta}_0) = \sigma_\varepsilon^2 \left( \frac{1}{n} + \frac{\bar{x}^2}{n \hat{\sigma}_X^2} \right)$	$t_{j,\text{obs}} = \frac{\hat{\beta}_j - \beta_{j,H_0}}{\widehat{SE}(\hat{\beta}_j)}, \quad j = 0, 1$
Chi-quadro $\chi^2$		
$\chi_{\text{obs}}^2 = \sum_{i=1}^I \sum_{j=1}^J \frac{(n_{ij} - n_{ij}^*)^2}{n_{ij}^*}$		